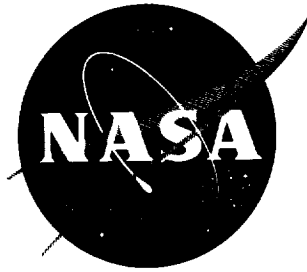


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## TECHNICAL NOTE

D-1487

EFFECTS OF LEADING-EDGE BLUNTNESS ON  
FLUTTER CHARACTERISTICS OF SOME SQUARE-PLANFORM  
DOUBLE-WEDGE AIRFOILS AT A MACH NUMBER OF 15.4

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EFFECTS OF LEADING-EDGE BLUNTNESS ON  
FLUTTER CHARACTERISTICS OF SOME SQUARE-PLANFORM  
DOUBLE-WEDGE AIRFOILS AT A MACH NUMBER OF 15.4

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SUMMARY

Results are presented from a wind-tunnel investigation in helium flow at a Mach number of 15.4. The models were square-planform, double-wedge, shaft-mounted airfoils with leading- and trailing-edge radii of 0, 1, 3, and 6 percent chord. In general, the tests indicate that bluntness effects on the model flutter characteristics are stabilizing as the leading-edge radius is increased from 0 to 6 percent of the chord, but then become destabilizing with further increase in bluntness.

Results of flutter calculations made by using Newtonian theory aerodynamics and a combination of Newtonian theory and piston theory aerodynamics in conjunction with an uncoupled two-mode analysis are compared with experimental results. The piston-theory results accurately predicted flutter speeds for the models with sharp leading edge. The Newtonian theory, although conservative, gave better predictions than the Newtonian-piston theory for the blunt-leading-edge models.

INTRODUCTION

Airfoils on very high-performance aircraft and missiles frequently have rounded leading edges to alleviate the aerodynamic-heating problem. It is pertinent, therefore, to investigate the effect of bluntness on the flutter of airfoils in the hypersonic range. Double-wedge models have often been used in high-speed flutter investigations (refs. 1 to 4) and the effect of leading-edge bluntness on the flutter of such models has been studied in the Mach number region from 0.7 to 36 (ref. 1). It is the purpose of this paper to extend the study of reference 1 to a Mach number of 15.4 upon the basis of tests of double-wedge models in helium, in which the bluntness of the leading edges was varied systematically over a range of radii from 0 to 6 percent of the chord.

In addition to further experimental studies, the need exists for evaluation of available analytical methods for the prediction of aeroelastic phenomena at high speeds. In this report two-degree-of-freedom flutter calculations were made for the various models tested by using the first two uncoupled modes in conjunction with Newtonian theory aerodynamics and a combination of Newtonian and piston

theory aerodynamics. These two theoretical methods were evaluated by comparison with the experimental results.

#### SYMBOLS

b	wing semispan, ft
$f_f$	flutter frequency, cps
$f_h$	flapping frequency, cps
$f_n$	natural frequency of nth mode ( $n = 1$ and $2$ ), cps
$f_\alpha$	pitching frequency (bending degree of freedom restrained), cps
$I_\alpha$	mass moment of inertia about pitch axis, slug-ft <sup>2</sup>
m	mass, slugs
$r_\alpha$	radius of gyration of model, referred to pitch axis, $\sqrt{\frac{I_\alpha}{mb^2}}$ , nondimensional
V	free-stream velocity, ft/sec
$x_0$	pitch-axis location measured from leading edge, percent chord
$x_{cg}$	distance from leading edge to center of gravity, percent chord
$y_{cg}$	distance from root chord to center of gravity, percent semispan
$\mu$	nondimensional mass ratio (ratio of mass of model to mass of volume of test medium contained in a solid generated by revolving each chord about its midpoint, length of solid being wing semispan)
$\omega_f$	flutter frequency, radians/sec
$\omega_n$	frequency of nth mode ( $n = 1, 2$ ), radians/sec

#### Subscripts:

av	average
div	divergence
exp	experimental results
th	theoretical results

## APPARATUS

The tests were performed in the 24-inch-diameter nozzle of the Langley hypersonic aeroelasticity tunnel, which uses helium as a test medium. The tunnel has a contoured nozzle designed to generate a uniform flow at a Mach number of about 15.4. A photograph of this blowdown tunnel is shown in figure 1.

Helium is supplied to the stagnation chamber at pressures up to 1,200 lb/sq in., from which dynamic pressures up to 595 lb/sq ft are obtainable. The downstream end of the tunnel is connected to a vacuum chamber which can be operated at pressures as low as 1/2 inch of mercury absolute. With the available high-pressure helium supply, test runs were of approximately 5-second duration.

Test-section Mach number distributions as obtained from impact-tube surveys are presented in figures 2(a) and 2(b). Figure 2(a) shows that the average Mach number at a given point was about 15.4. Also shown is that the Mach number remained practically constant for a given stagnation pressure. Figure 2(b) shows that there was little variation of Mach number over the length of the test section.

The models were mounted on a reflection plane which was supported 6.8 inches from the tunnel wall as shown in figure 3. The reflection-plane support structure is designed to insure that the model was out of the tunnel boundary layer and in a region of uniform flow. A sketch of the tunnel test section showing its overall dimensions and the location of the model and its support structure is presented in figure 4. Mach number surveys have been made from the reflection plane across the diameter of the test section along the model location. The results are shown in figure 5. It appears that the reflection-plane leading edge was in a region of undisturbed flow; however, a disturbed region was building up along the reflection-plane surface as the flow moved rearward. Even so, in the vicinity of the model trailing edge, the disturbed region covered less than 15 percent of the span. The tip of the model was in uniform flow and not in the boundary layer from the opposite tunnel wall.

Provision was made for a clamping device which was located at the junction of the model shaft and reflection plane in the support structure. This clamping device was used to restrain the model during the tunnel starting transient, and so to avoid destruction of the model when flutter occurred. Thus the same model could be used for more than one test.

## MODELS

The two series of models tested each had semispan aspect ratios of 1.0, zero sweep, double-wedge profile shapes, and no taper. The difference between the two series was that one had a 10-inch semispan whereas the other had a 6-inch semispan. Each series consisted of four models of varying leading-edge bluntness; they had leading- and trailing-edge radii of 0, 1, 3, and 6 percent of their chord. A photograph of the 10-inch models is shown in figure 6. The models were supported by a shaft which was an integral part of the aluminum-alloy core of the

model and which was clamped at the tunnel wall. Holes were drilled in the core and lead strips were added in order to achieve the desired mass and inertia properties. Then balsa wood was glued to the core to form the airfoil contour. The model construction is shown in figure 7. The models were designed as rigid bodies mounted on a soft spring (the shaft) in order to provide a simple model with well-defined structural properties. Therefore, the structural variables were isolated and the aerodynamic effects more pronounced.

## PHYSICAL PARAMETERS

The mass parameters of the models are listed in table I along with pertinent dimensions. The mass of the model shaft is not included in the data shown. The pitch axis of all the models was at the 35-percent-chord position with the plane center of gravity located at  $53.5(\pm 0.9)$  percent chord and  $50.0(\pm 1.5)$  percent span. All models were vibrated with an interrupted-air-jet shaker to determine the natural frequencies and nodal patterns. Typical nodal patterns for the models are shown in figure 8. In all cases examined, the third and fourth natural frequencies were well above the first and second natural frequencies. The first two coupled frequencies as well as the first two uncoupled frequencies are listed in table I. The first uncoupled frequency, flapping, was calculated by using the measured mass properties. The second uncoupled frequency, pitching, was found experimentally. Because the second natural node line was skewed, it was necessary to restrict the model deflection at an assumed pitch-axis location, 35 percent chord at the model tip, in order to measure the uncoupled pitching frequency. The first two uncoupled mode shapes for the models were determined in the following manner: For the flapping mode the model was vibrated at its first natural frequency by means of an air shaker, and the amplitude of vibration was measured at various stations with time-exposure photographs. This mode shape is presented in figure 9(a). Because a slight amount of pitching is evident, the model was assumed to be rigid and the deflection along the 50-percent-chord line (center-of-gravity location) was used in the calculations. For the pitching mode the model was vibrated in its restricted uncoupled pitching mode, and time-exposure photographs were used to measure the deflection. The pitching-mode shape is presented in figure 9(b) and was used in the flutter calculations. In addition, the fundamental uncoupled mode shape was calculated for a system consisting of a rigid beam on a flexible, weightless shaft and the result agreed well with the experimentally determined uncoupled flapping-mode shape.

## TEST PROCEDURE

Models were mounted in the test section at zero angle of attack. After installation in the tunnel and just prior to the test run, the measurements for the first two natural frequencies of the model were checked. The tunnel was then evacuated to a low pressure. The model was restrained, and a control valve upstream of the test section was opened and flow established at a low dynamic pressure. At this time the model was released and, with the Mach number remaining constant, dynamic pressure was increased until flutter was encountered or the

Maximum tunnel operating conditions were reached. At that point the model was again restrained and the tunnel flow stopped. Stagnation temperature and pressure were recorded on an oscillograph throughout the test. Signals from resistance-type strain gages mounted on the model shaft were also recorded and their response was used to determine the occurrence of flutter and the flutter frequency. These data were later correlated with the tunnel conditions. High-speed motion pictures of the flutter of most of the models were obtained.

## RESULTS AND DISCUSSION

### Experimental Investigation

The basic data from the tests are presented in table II. The test-section conditions at flutter as well as the flutter frequency ratio  $\omega_f/\omega_2$  and velocity-index parameter  $V/b\omega_2\sqrt{\mu}$  are listed for each test run. The experimental results from table II are presented in figures 10 and 11 as the variation of the velocity-index parameter and frequency ratio with leading-edge radius. In figure 12, some of the data of reference 1 are combined with the present data and presented as the variation of velocity-index parameter  $V/b\omega_2\sqrt{\mu}$  with Mach number for the various models.

Examination of the data for the 10-inch model in figure 10 reveals that the flutter speed increases as the leading-edge radius is increased from 0 to 1 percent of the chord, and then the trend reverses; that is, the flutter speed decreases with further bluntness. During tests of the 10-inch model with a leading-edge radius of 6 percent chord, the tunnel would not start; that is, the flow could not be established in the test section at  $M = 15.4$ .

In an attempt to investigate the 6-percent-chord leading-edge radius, and also to explore size effects, the 6-inch-chord models were constructed and tested. The flutter trend remained the same for the models with the 0-, 1-, and 3-percent-chord leading-edge radii, as can be seen in figure 10. However, no flutter was encountered for the 6-percent-chord leading-edge models; instead the model diverged. The divergence was quite abrupt, the model striking the reflection lane with little or no oscillatory displacement.

The flutter mode was a combination of the flapping and pitching natural modes. Figure 11 shows the flutter frequency ratio as a function of leading-edge radii. For the models with sharp and 1-percent-chord leading edges, the flutter frequency ratios ranged from 0.47 to 0.59, whereas for the models with 3-percent-chord radii, it decreased to between 0.31 and 0.37. From this result and from observations of the films of the test it is believed that for the models with 3-percent-chord radius the flutter condition was approaching the divergence condition and thus the flutter frequency was forced toward zero.

In figure 12, some of the results of reference 1 have been combined with those reported in this paper to show the variation of the velocity-index parameter over a wide range of Mach number. The models with sharp and 1-percent-chord radius exhibit the same trend of consistently increasing values of the

parameter with increasing Mach number. The model with 3-percent-chord radius warrants special attention, for in this case the velocity-index parameter, rather than increasing with Mach number, reverses the trend between  $M = 7.0$  and  $15.4$ ; and at  $M = 15.4$  the parameter has the same value as at  $M = 2.6$ . The models with leading-edge radii of 6 percent of the chord diverged at all Mach numbers above about 1.6. At a Mach number of 15.4, the value of the velocity-index parameter for divergence was about the same as at Mach 1.6. It should be noted that over the Mach number range the minimum value of the velocity-index parameter occurred near  $M = 1$ .

### Theoretical Investigation

Lighthill, in reference 5, developed a simplified aerodynamic theory which has become known as "piston theory." Ashley and Zartarian (ref. 6) have applied it to the flutter problem. They point out that the theory does not consider three-dimensional effects, but it should be noted that with increase in Mach number these effects should become less important. In addition, a requirement for good accuracy is that the downwash velocity at the wing surface divided by the speed of sound must be less than 1. This requirement, besides being a limit on airfoil thickness, also implies that piston theory will not be applicable near the leading edge of blunt-nosed airfoils where the surface slopes are large. It has been suggested in reference 7 that the use of Newtonian theory would remove the limitation due to bluntness. The Newtonian theory would be used over the leading-edge radius and piston theory over the remainder of the airfoil. Newton theory, even though it is based upon simple impact considerations, has given good aerodynamic predictions in hypersonic flow (ref. 8).

Two-degree-of-freedom flutter calculations were made for the models by using the first two uncoupled modes in conjunction with modified Newtonian-piston theory and modified Newtonian theory aerodynamics. The calculated uncoupled flapping frequencies and the experimentally determined pitching frequencies given in table I were used in the solution of the flutter determinant. Generalized mass terms were calculated from the experimentally measured mass, moment of inertia about the pitch axis, and center-of-gravity position as given in table I. The mass of the shaft was not included, and the panel mass was assumed to be uniform over the span, which was very nearly the case. The results of these calculations are listed in table III and presented in figures 13 and 14. Figure 13 presents the ratio of experimental to calculated flutter speed as a function of leading-edge bluntness. In figure 13(a) the calculated flutter-speed data are presented for the 10-inch-chord models. There was excellent agreement between experiment and piston theory for the sharp-leading-edge models, whereas the Newtonian theory was unconservative. With increase in bluntness both the Newtonian-piston and Newtonian theories became conservative, with the Newtonian theory giving slightly better agreement with the experiment. Figure 13(b) presents the same data for the 6-inch-chord models with about the same results; although the agreement for the blunt airfoils is better.

The ratios of experimental to theoretical flutter frequency are presented in figure 14 as a function of leading-edge radius. The Newtonian-piston theory predicted the flutter frequency somewhat more accurately, although neither theory



dicted the decrease in flutter frequency which occurred for the 3-percent-leading-edge model.

In an effort to investigate the divergence of some of the models analytically, the Newtonian theory flutter determinant was expanded and the flutter frequency set equal to zero. These divergence results are presented in figure 15 along with the Newtonian flutter theory and the average experimental results. According to the theory the flutter speed of each model was lower than its divergence speed. It should be noted that the calculated divergence speed was approaching the flutter speed with increase in model bluntness.

#### SUMMARY OF RESULTS

Wind-tunnel tests at a Mach number  $M$  of 15.4 on square-planform, all-movable-control-type models having leading- and trailing-edge radii from 0 to 6 percent chord and double-wedge profiles indicated a definite effect of airfoil bluntness on their aeroelastic characteristics. The tests indicated that bluntness effects were stabilizing as the leading-edge radius was increased from 0 to about 1 percent of the chord. A further increase in bluntness had a destabilizing effect on the flutter characteristics.

For the models with sharp leading edges and 1-percent-chord leading-edge radii the stabilizing trend was consistent with data obtained at lower Mach numbers in NASA TN D-984. For the 3-percent-chord leading-edge model there was a reversal in trend with Mach number between  $M = 7.0$  and  $M = 15.4$ . Within this Mach number range there was a destabilizing trend, and at  $M = 15.4$  the model countered flutter at about the same velocity-index parameter as at  $M = 2.6$ . This decrease in stability was believed to be due to the fact that the flutter speed was close to the divergence speed. At  $M = 15.4$ , increasing the airfoil bluntness to 6 percent of the chord led to divergence, as it did at lower Mach numbers. However, the velocity-index parameter for divergence at  $M = 15.4$  increased to about the same value as at  $M = 1.6$ .

Flutter calculations made by using Newtonian theory aerodynamics and a combination of Newtonian theory and piston theory aerodynamics, both in conjunction with an uncoupled two-mode analysis, indicated that the Newtonian-piston theory, though conservative, more closely predicted the flutter speed for the models with blunt leading edges. Neither theory predicted the flutter frequency well.

The Newtonian theory failed to predict divergence for the 6-percent-chord leading-edge model, but instead predicted a flutter speed lower than the divergence speed. The theory did show that the divergence speed was approaching the flutter speed with increasing leading-edge bluntness.

Langley Research Center,  
National Aeronautics and Space Administration,  
Langley Station, Hampton, Va., July 17, 1962.

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$[x_0 = 35 \text{ percent chord}]$

Model (a)	Mass, m, slugs	$x_{cg}$ , % chord	$y_{cg}$ , % semispan	$I_{\omega}$ slug-ft <sup>2</sup>	$r_a^2$	Wing semichord, b, ft	Wing semispan, ft	Maximum thickness, percent chord	$f_1$ , cps	$f_2$ , cps	$f_{\omega}$ , cps	$f_1/f_2$	$f_1/f_a$	$f_h$ , cps
0-A-10-1	0.0348	52.6	49.7	2.7342 $\times 10^{-3}$	0.452	0.417	0.833	9.0	6.0	21.3	17.8	0.282	0.337	7.2
0-B-10-1	0.0422	53.5	49.8	3.3250	.453				7.4	25.3	21.8	.292	.339	9.3
0-C-10-1	0.0486	53.1	49.0	3.7133	.440				9.1	32.3	26.7	.282	.341	10.9
0-A-10-2	0.0486	53.1	49.0	3.7133	.440				5.5	19.8	15.7	.278	.350	6.1
0-A-10-3	0.0348	52.6	49.7	2.7342	.452				6.4	22.2	18.2	.288	.351	7.2
1-A-10-1	0.0364	53.0	50.5	2.8800	.455			11.0	5.9	20.0	17.8	.295	.331	7.1
1-B-10-1	0.0465	53.4	50.4	3.6092	.446				7.3	26.8	22.4	.272	.326	8.7
1-C-10-1	0.0495	53.2	49.1	3.8650	.449				9.1	31.9	26.3	.285	.346	10.9
1-A-10-2	0.0495	53.2	49.1	3.8650	.449				5.4	19.7	16.5	.277	.330	6.1
3-A-10-1	0.0429	52.6	50.0	3.3133	.444			14.0	5.7	21.1	17.9	.270	.318	6.5
3-B-10-1	0.0502	52.7	51.5	3.8158	.437				6.8	25.2	21.2	.270	.321	8.4
3-C-10-1	0.0552	53.5	51.4	4.3133	.450				8.5	31.3	26.1	.272	.326	10.2
3-A-10-2	0.0552	53.5	51.4	4.3133	.450				5.2	19.3	16.5	.269	.315	6.2
6-A-10-1	0.0496	52.9	51.4	3.9258	.455			20.0	5.2	19.5	16.5	.267	.315	6.2
6-B-10-1	0.0540	52.9	51.0	4.4008	.469				6.7	24.0	20.5	.279	.326	8.0
6-C-10-1	0.0601	53.6	51.1	4.9475	.473				8.3	29.6	25.0	.280	.332	9.9
0-A-6-1	0.0167	53.3	49.2	.445	.426	.250	.500	9.0	6.3	25.5	21.0	.247	.300	6.6
0-A-6-2	0.0170	54.1	49.2	.458	.431				6.2	25.2	20.4	.246	.304	6.5
0-A-6-3	0.0163	54.3	50.8	.434	.426				6.4	25.8	20.9	.248	.306	6.7
1-A-6-1	0.0165	54.3	50.0	.442	.429			11.0	6.3	24.9	20.5	.253	.307	6.6
1-A-6-2	0.0170	54.3	49.3	.456	.429				6.5	25.5	21.3	.255	.305	6.6
1-A-6-3	0.0168	53.3	50.0	.441	.420				6.3	24.8	20.5	.254	.307	6.6
3-A-6-1	0.0175	53.3	50.0	.438	.406			14.0	6.4	26.1	21.4	.245	.300	6.5
3-A-6-2	0.0167	53.4	49.5	.430	.412				6.4	26.3	21.4	.243	.300	6.6
3-A-6-3	0.0172	54.2	49.5	.443	.412				6.4	26.5	21.3	.242	.300	6.6
6-A-6-1	0.0185	53.2	51.5	.464	.401			20.0	6.1	25.9	20.2	.236	.302	6.4
6-A-6-2	0.0184	53.2	50.0	.460	.400				6.0	24.8	19.9	.242	.302	6.3
6-A-6-3	0.0183	53.2	50.0	.456	.400				5.9	24.2	19.7	.244	.300	6.2
6-A-6-4	0.0233	53.2	50.5	.582	.400				5.7	21.2	17.9	.269	.318	6.0

<sup>a</sup>In the model designation the first integer indicates leading-edge radius in percent chord; the letter indicates the stiffness level of the model (where  $A < B < C$ ); the next number is the chord and semispan in inches; and the last number is the model number in a group of similar models.

TABLE II.- COMPILATION OF TEST RESULTS

Model (a)	Run	Mach number	Dynamic pressure, lb/sq ft	Density, slugs/cu ft	Speed of sound, ft/sec	$\mu$	V, ft/sec	$\omega_2$ , radians/sec	$V/b\omega_2\sqrt{\mu}$	$\omega_T$ , radians/sec	$\omega_T/\omega_2$
0-B-10-1	1	15.50	512	$2.817 \times 10^{-5}$	389	3,291.7	6,029.5	159.0	1.585	81.7	0.514
0-A-10-3	2	15.30	306	1.889	372	4,046.5	5,691.6	139.5	1.538	82.0	.588
0-A-10-2	3	15.20	287	1.478	410	7,221.4	6,232.0	124.4	1.414	66.9	.538
1-A-10-1	4	15.40	401	1.992	412	4,013.2	6,344.8	125.7	1.911	69.8	.555
1-A-10-1	5	15.40	398	1.987	411	4,026.5	6,329.4	125.7	1.903	-----	-----
1-A-10-2	6	15.40	432	2.277	400	4,778.0	6,160.0	123.8	1.726	72.3	.584
3-B-10-1	7	15.40	405	1.856	429	5,940.8	6,606.6	158.3	1.298	54.0	.341
3-B-10-1	8	15.50	474	2.466	400	4,474.2	6,200.0	158.3	1.404	55.9	.353
0-A-6-1	9	15.30	313	1.492	423	11,376.0	6,471.9	160.22	1.515	78.5	.490
1-A-6-2	10	15.45	429	2.213	403	7,823.3	6,226.4	160.22	1.757	75.4	.471
1-A-6-3	11	15.30	340	1.728	410	9,899.8	6,273.0	155.80	1.619	77.3	.496
3-A-6-1	12	15.20	280	1.361	422	13,089.0	6,414.4	163.99	1.368	59.7	.364
3-A-6-2	13	15.20	297	1.444	422	11,777.2	6,414.4	165.25	1.431	52.5	.318
6-A-6-1	14	15.20	b292	1.361	431	13,836.9	b6,551.2	162.73	b1.369	-----	-----
6-A-6-1	15	15.00	b173	.933	406	20,196.5	b6,090.0	162.73	b1.053	-----	-----
6-A-6-2	16	15.00	b180	.961	408	19,491.5	b6,120.0	155.82	b1.125	-----	-----
6-A-6-4	17	15.35	b415	2.258	395	10,448.4	b6,063.3	133.2	b1.068	-----	-----

<sup>a</sup>In the model designation the first integer indicates leading-edge radius in percent chord; the letter indicates the stiffness level of the model (where A < B < C); the next number is the chord and semispan in inches; and the last number is the model number in a group of similar models.

<sup>b</sup>Divergent condition.

TABLE III.- COMPILATION OF THEORETICAL CALCULATIONS

Model	Run	Flutter calculations										Divergence calculations, Newtonian theory	
		Newtonian theory					Newtonian-piston theory						
		$V_{th}$ ft/sec	$\omega_f, th$ radians/sec	$\frac{V_{exp}}{V_{th}}$	$\frac{\omega_f, exp}{\omega_f, th}$	$V_{th}$ ft/sec	$\omega_f, th$ radians/sec	$\frac{V_{exp}}{V_{th}}$	$\frac{\omega_f, exp}{\omega_f, th}$	Divergent dynamic pressure, lb/sq ft	$\frac{V}{b\omega_2\sqrt{\mu}}$		
(a)	0-B-10-1	1	6,662.3	111.9	0.905	0.730	5,997.2	103.0	1.005	0.793	4,648	4.789	
	0-A-10-3	2	6,493.3	96.7	.877	.848	5,758.5	89.8	.988	.913	2,882	4.737	
	0-A-10-2	3	7,220.6	80.2	.863	.834	6,385.5	74.3	.976	.900	2,764	4.620	
	1-A-10-1	4	5,367.2	85.2	1.182	.819	4,952.9	79.4	1.281	.879	1,544	3.582	
	1-A-10-2	6	5,540.5	78.6	1.112	.920	5,025.0	73.6	1.226	.982	1,809	3.582	
	3-B-10-1	7	6,492.7	93.1	1.018	.580	6,164.4	90.0	1.072	.600	1,928	2.836	
	3-B-10-1	8	5,624.0	93.0	1.102	.601	5,345.4	89.9	1.160	.622	1,928	2.836	
	0-A-6-1	9	7,750.7	106.6	.835	.736	6,781.1	100.4	.954	.782	3,145	4.593	
	1-A-6-2	10	5,931.5	102.9	1.050	.733	5,390.3	97.2	1.155	.776	1,990	3.499	
	1-A-6-3	11	6,232.5	96.9	1.006	.798	5,684.0	91.4	1.104	.846	1,739	3.488	
	3-A-6-1	12	6,342.1	92.1	1.011	.648	5,916.8	89.9	1.084	.664	1,022	2.490	
	3-A-6-2	13	6,005.1	92.2	1.068	.569	5,607.2	88.8	1.144	.591	975	2.444	
	6-A-6-1	14	5,306.9	87.5	1.234	-----	5,096.3	86.5	1.285	-----	648	1.936	
	6-A-6-1	15	6,513.7	87.6	.935	-----	6,006.6	86.6	1.014	-----	648	1.928	
	6-A-6-2	16	6,223.9	87.0	.983	-----	5,913.0	86.3	1.035	-----	650	2.037	
	6-A-6-4	17	3,706.6	74.4	1.636	-----	3,537.1	74.3	1.714	-----	533	2.013	

<sup>a</sup>In the model designation the first integer indicates leading-edge radius in percent chord; the letter indicates the stiffness level of the model (where A < B < C); the next number is the chord and semispan in inches; and the last number is the model number in a group of similar models.

Leading-edge radius, % chord	$\left(\frac{V_{th}}{b\omega_2\sqrt{\mu}}\right)_{av}$ for -	
	Flutter	Divergence
0	1.714	4.685
1	1.654	3.565
3	1.531	2.600
6	.964	1.978

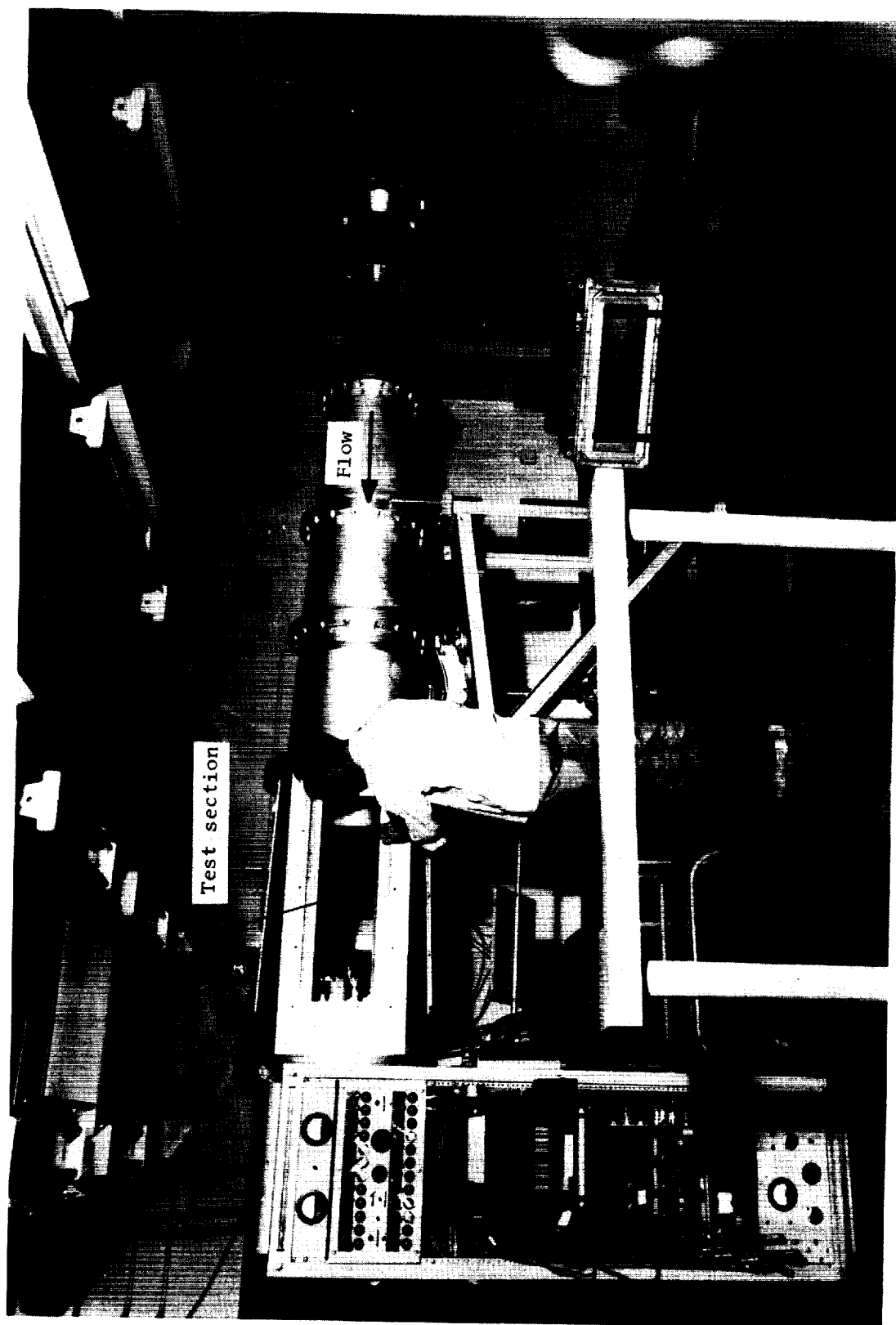
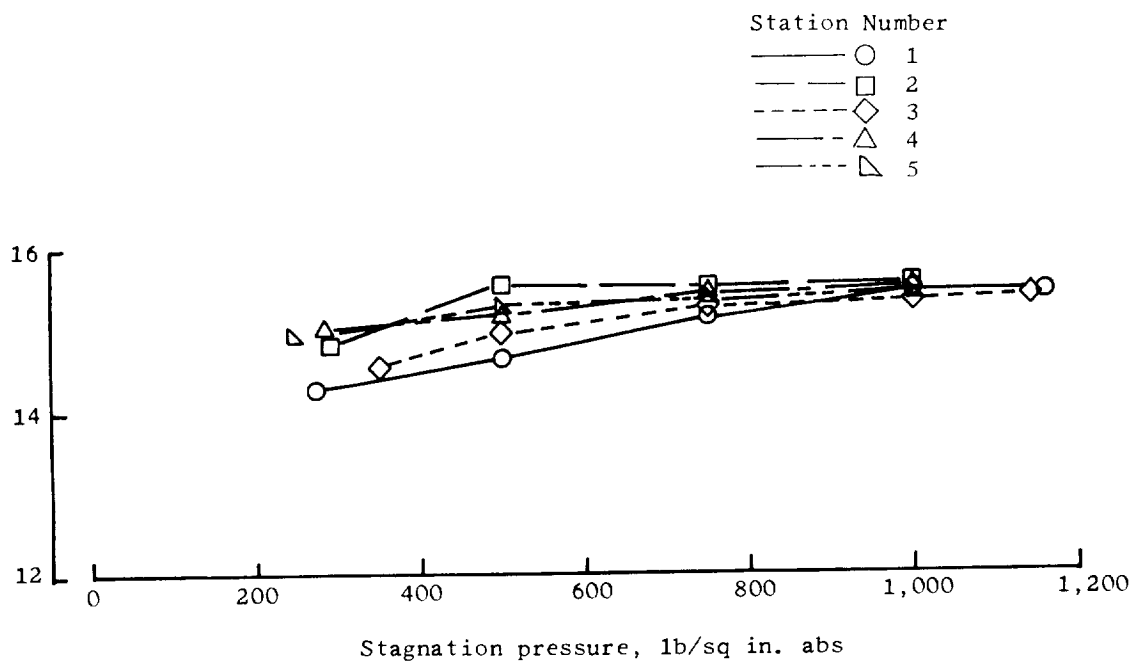
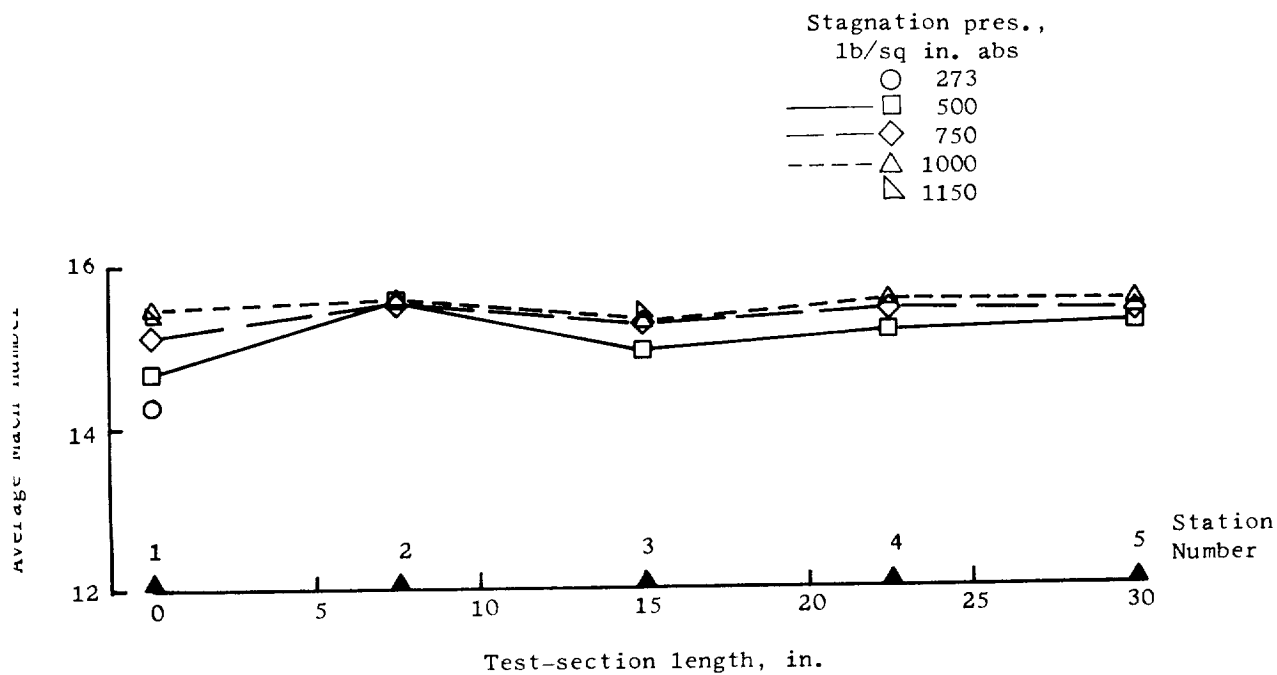


Figure 1.- Langley hypersonic aerolasticity tunnel. L-61-7414.1



(a)



(b)

Figure 2.- Mach number survey along tunnel test-section length.

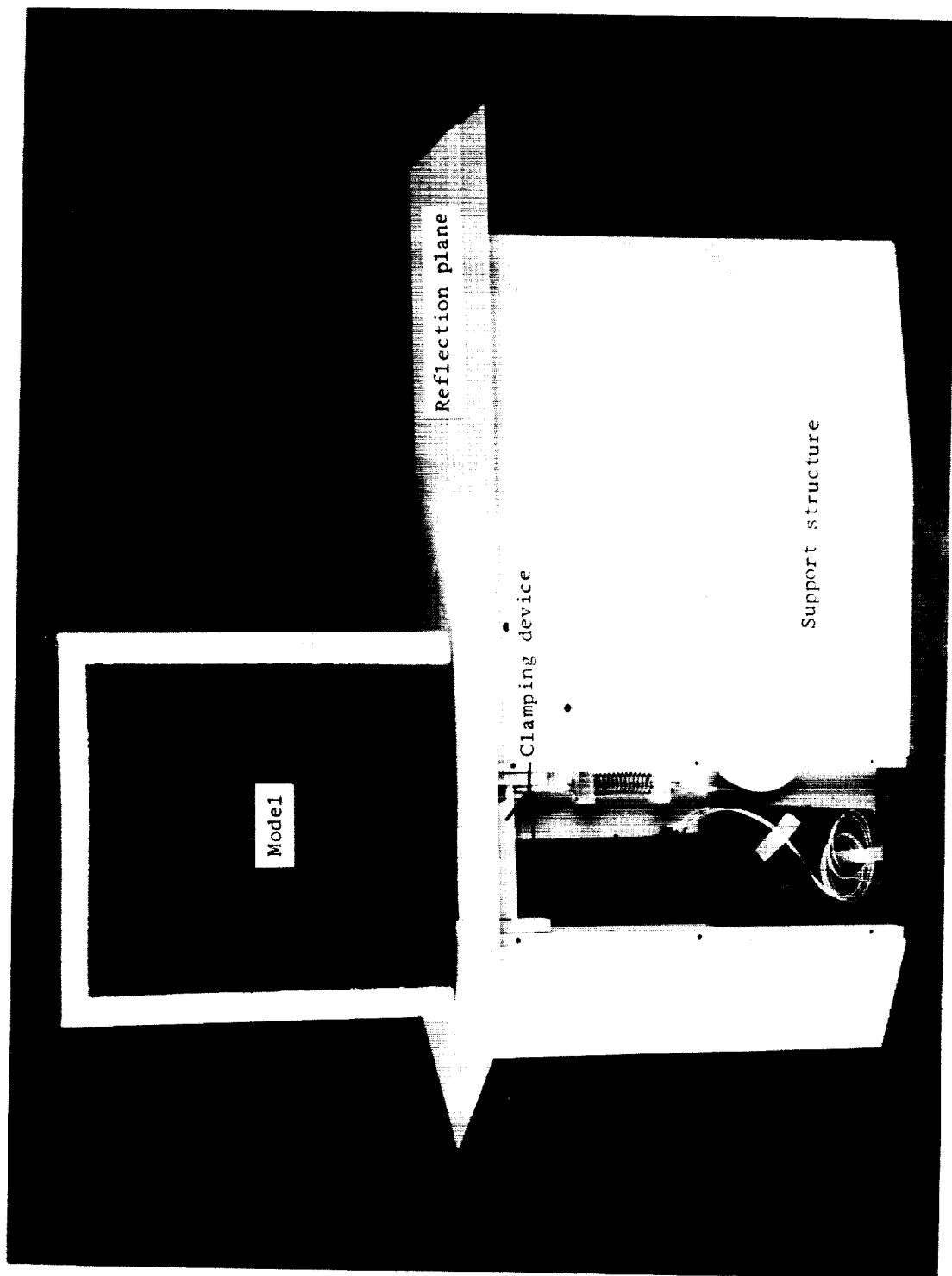


Figure 3.- Model support structure. L-62-3321.1



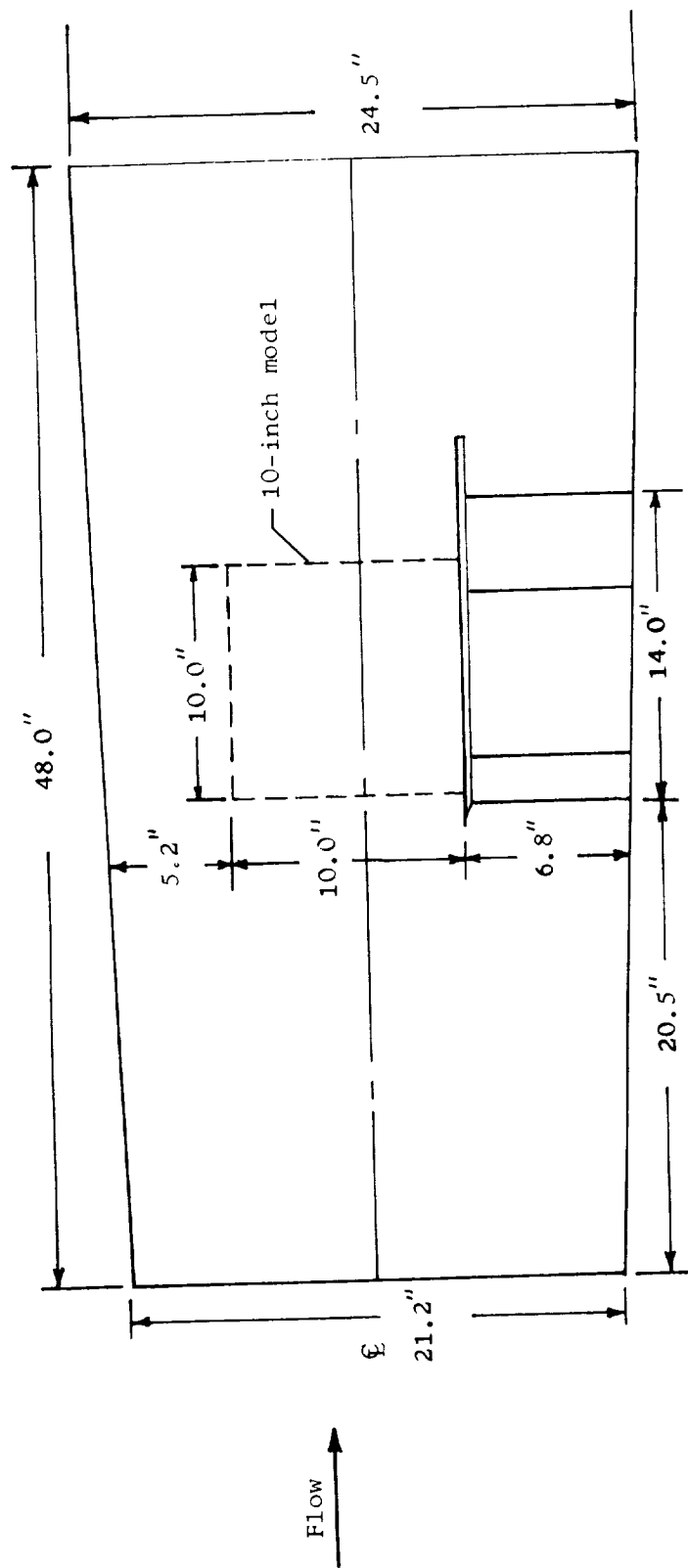


Figure 4.- Location of model support structure in tunnel test section. All dimensions are in inches.

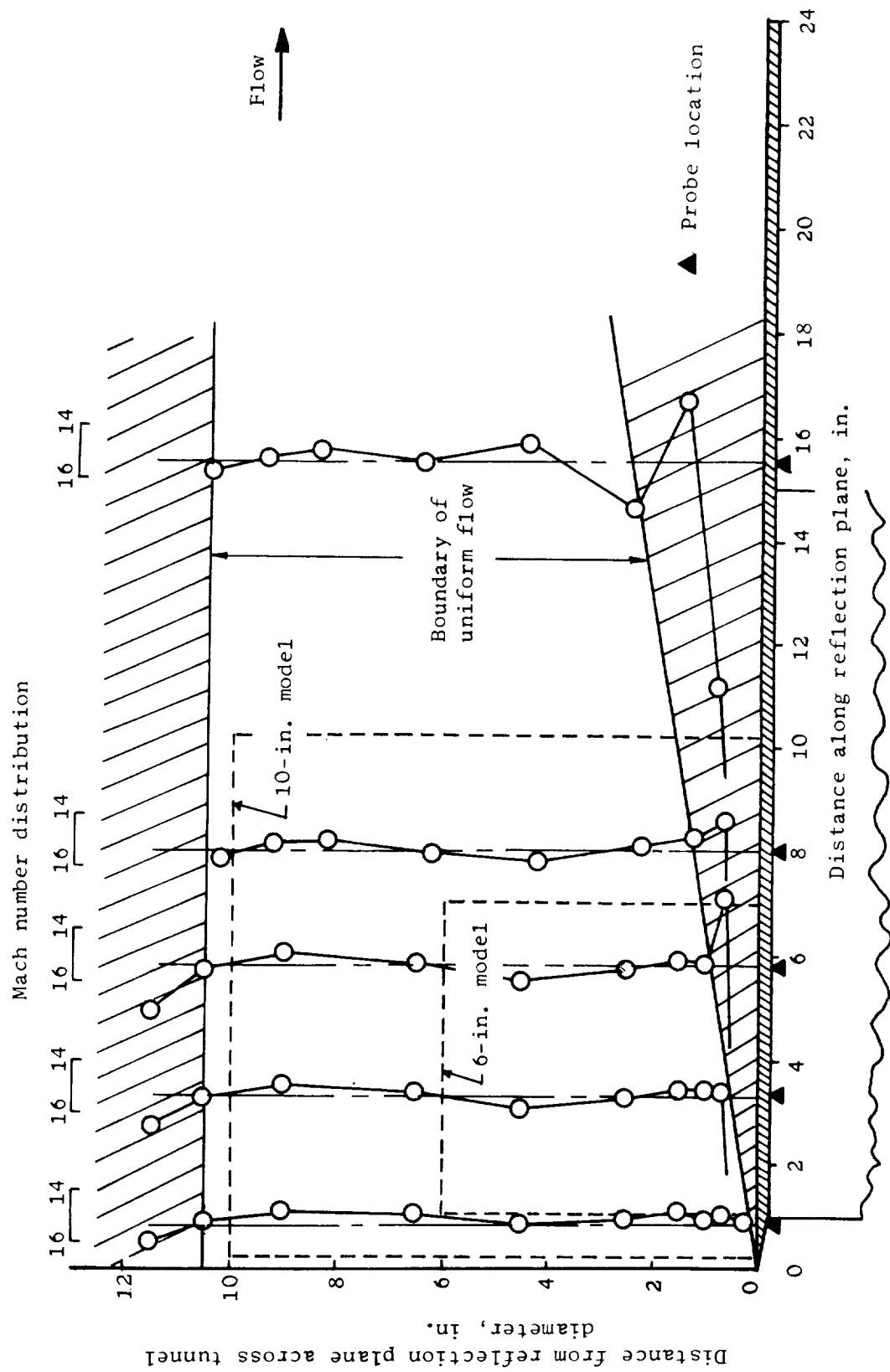


Figure 5.- Mach number survey in the plane of the model. Stagnation pressure, 750 lb/sq in.

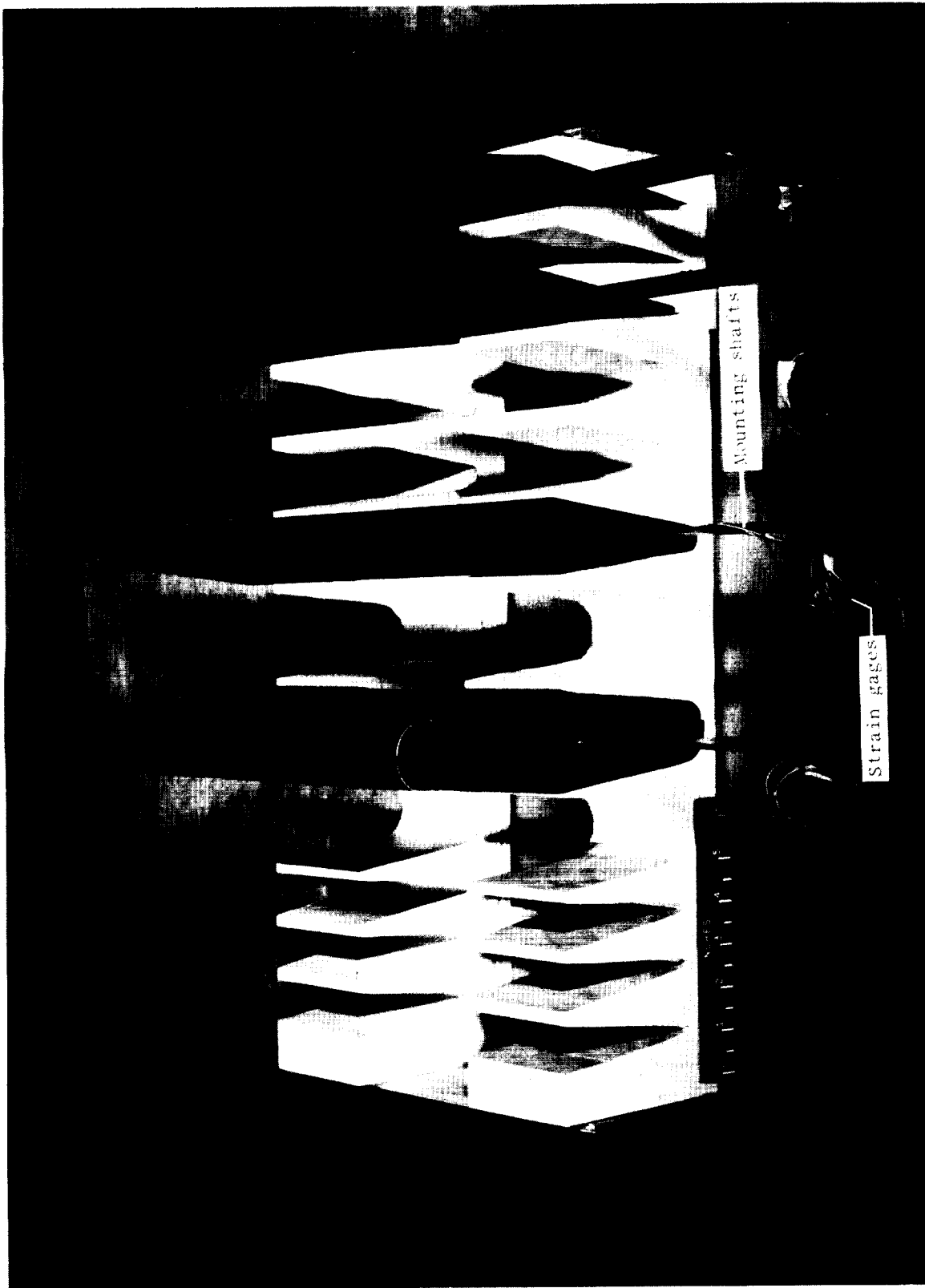


Figure 6.- Model profiles tested. L-61-1768.1

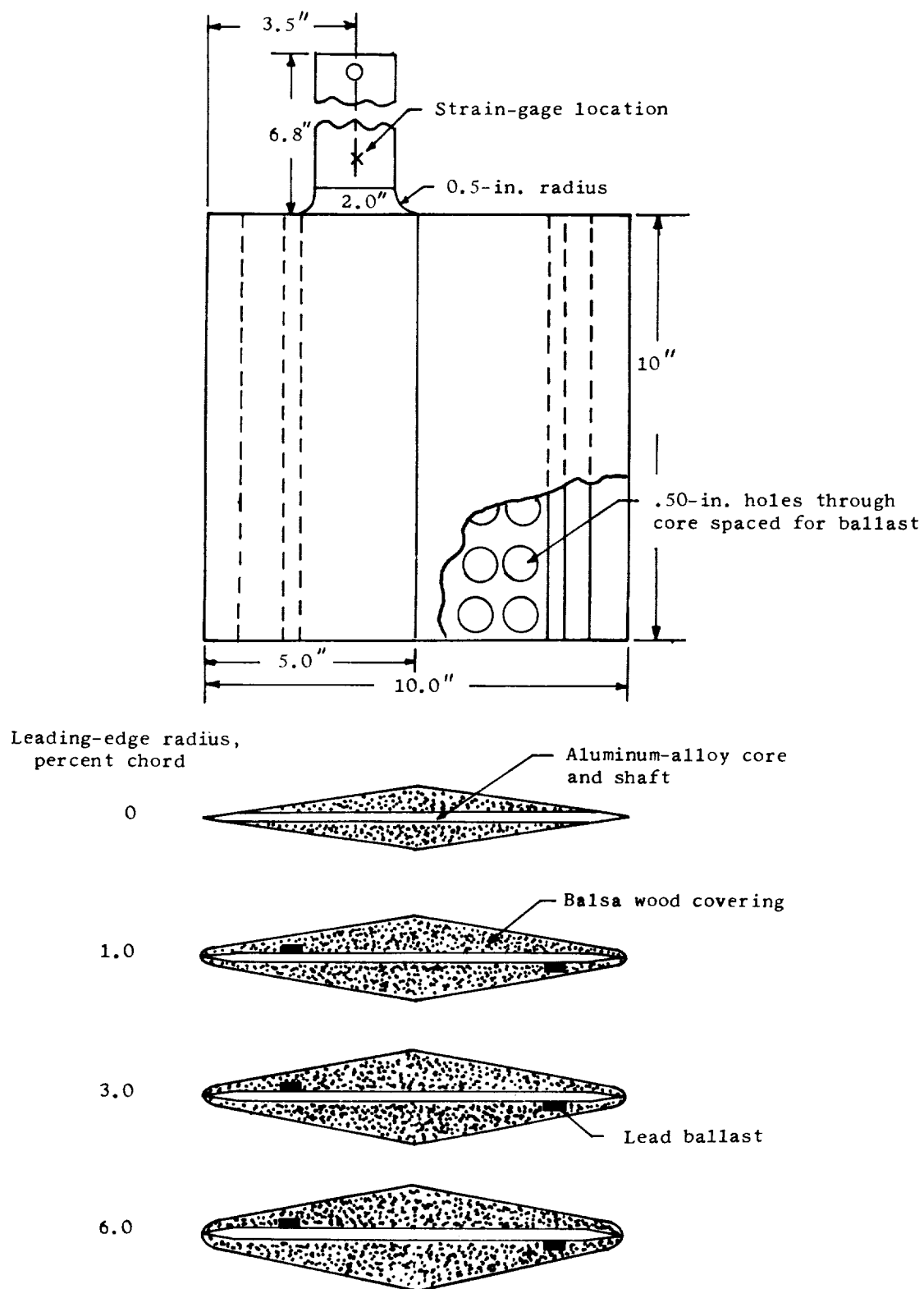


Figure 7.- Geometry and construction of 10-inch model series.

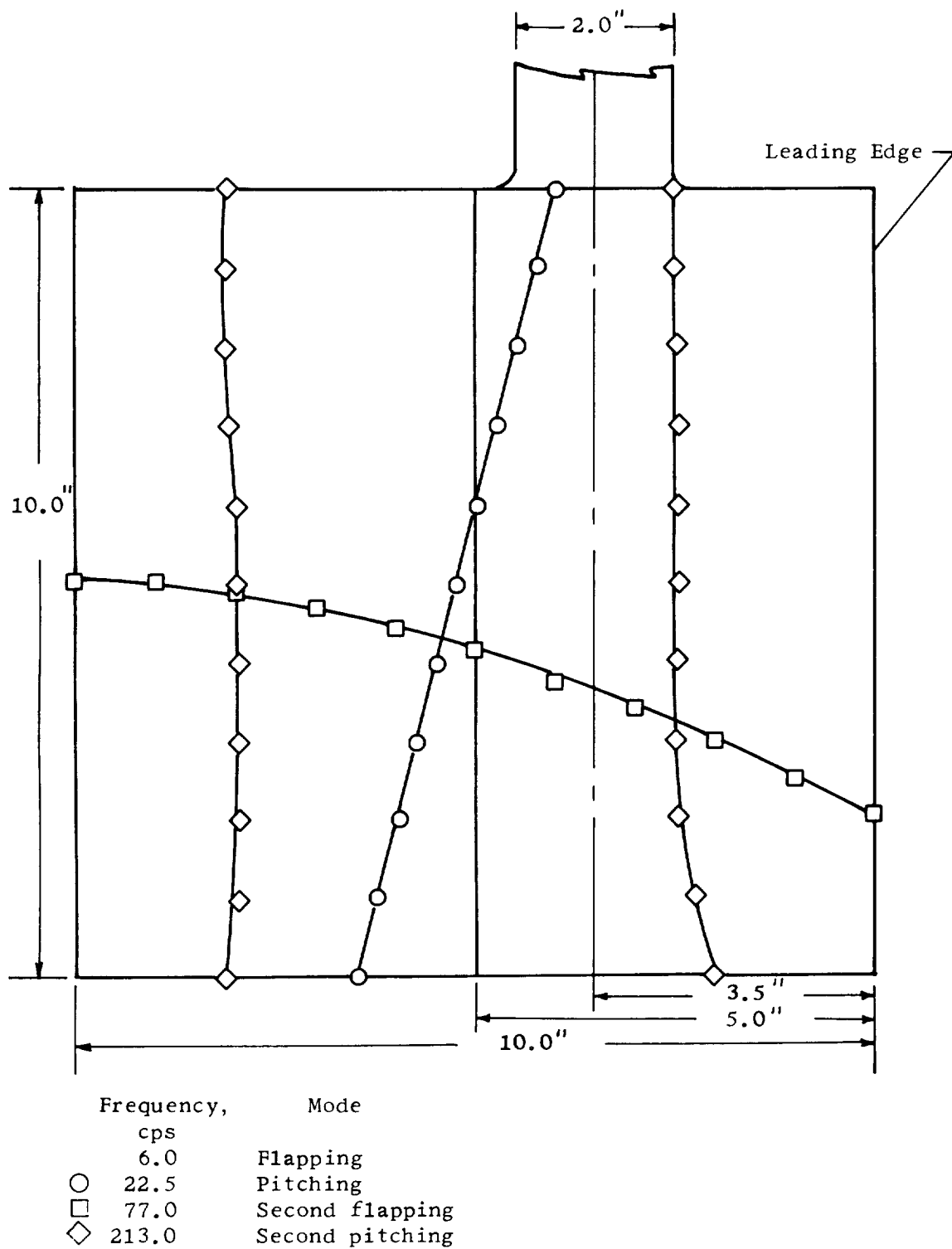
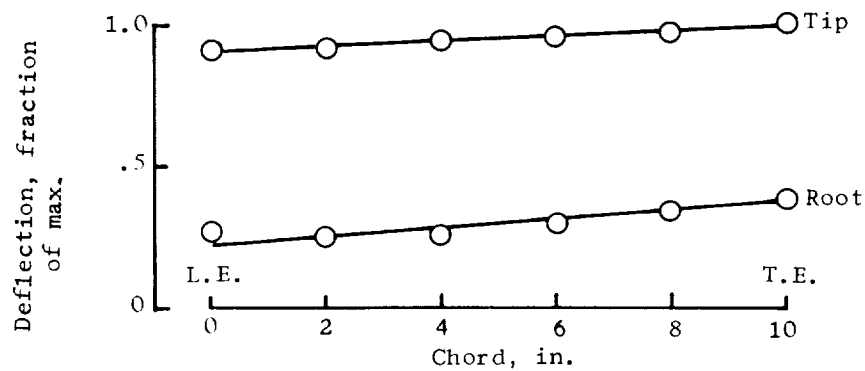
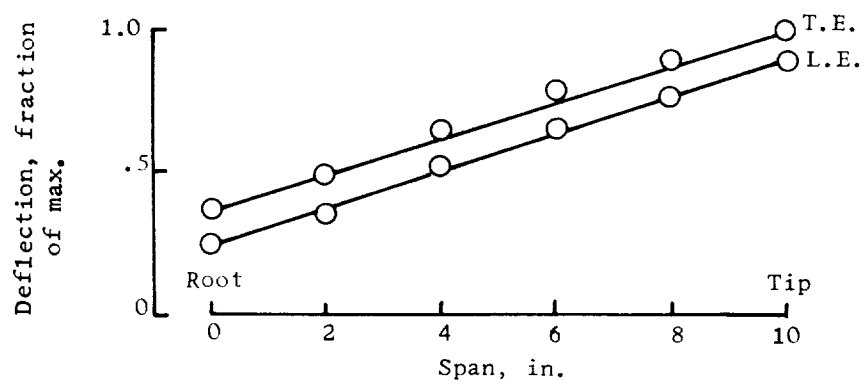
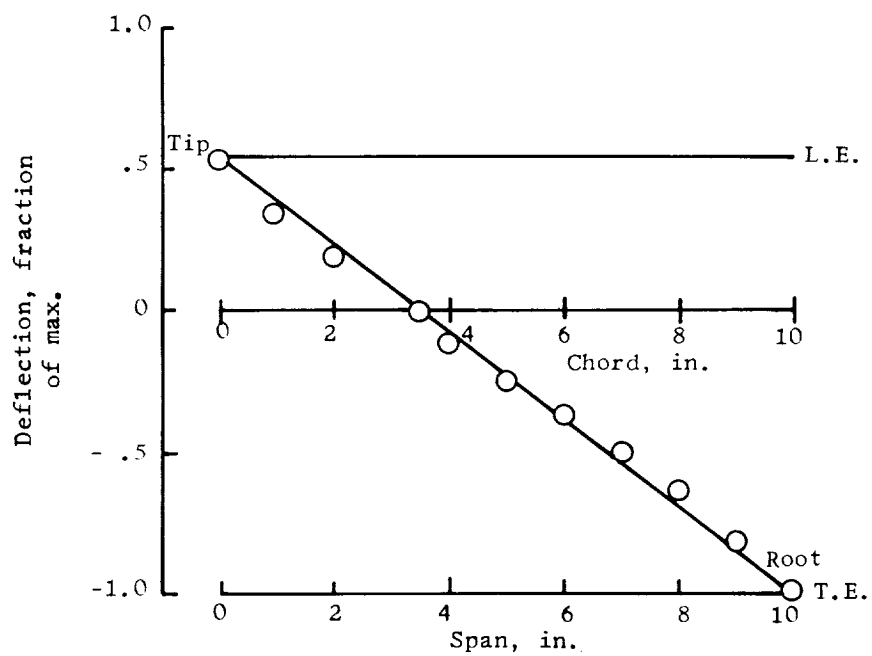


Figure 8.- Typical nodal patterns of models.



(a) Flapping mode.



(b) Uncoupled pitching mode.

Figure 9.- Typical mode shape of flapping and uncoupled pitching modes.

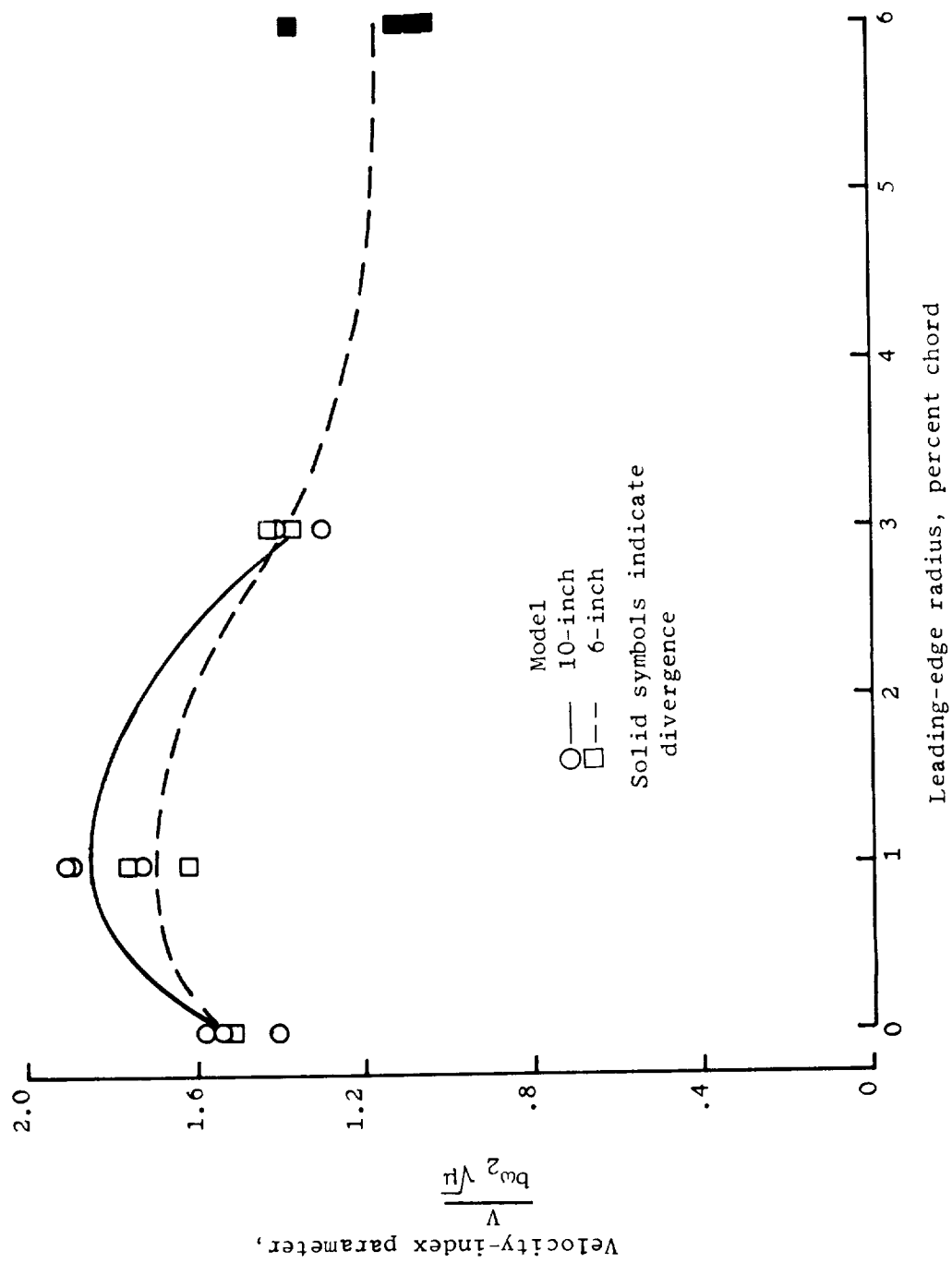


Figure 10.- Variation of velocity-index parameter as a function of leading-edge radius.

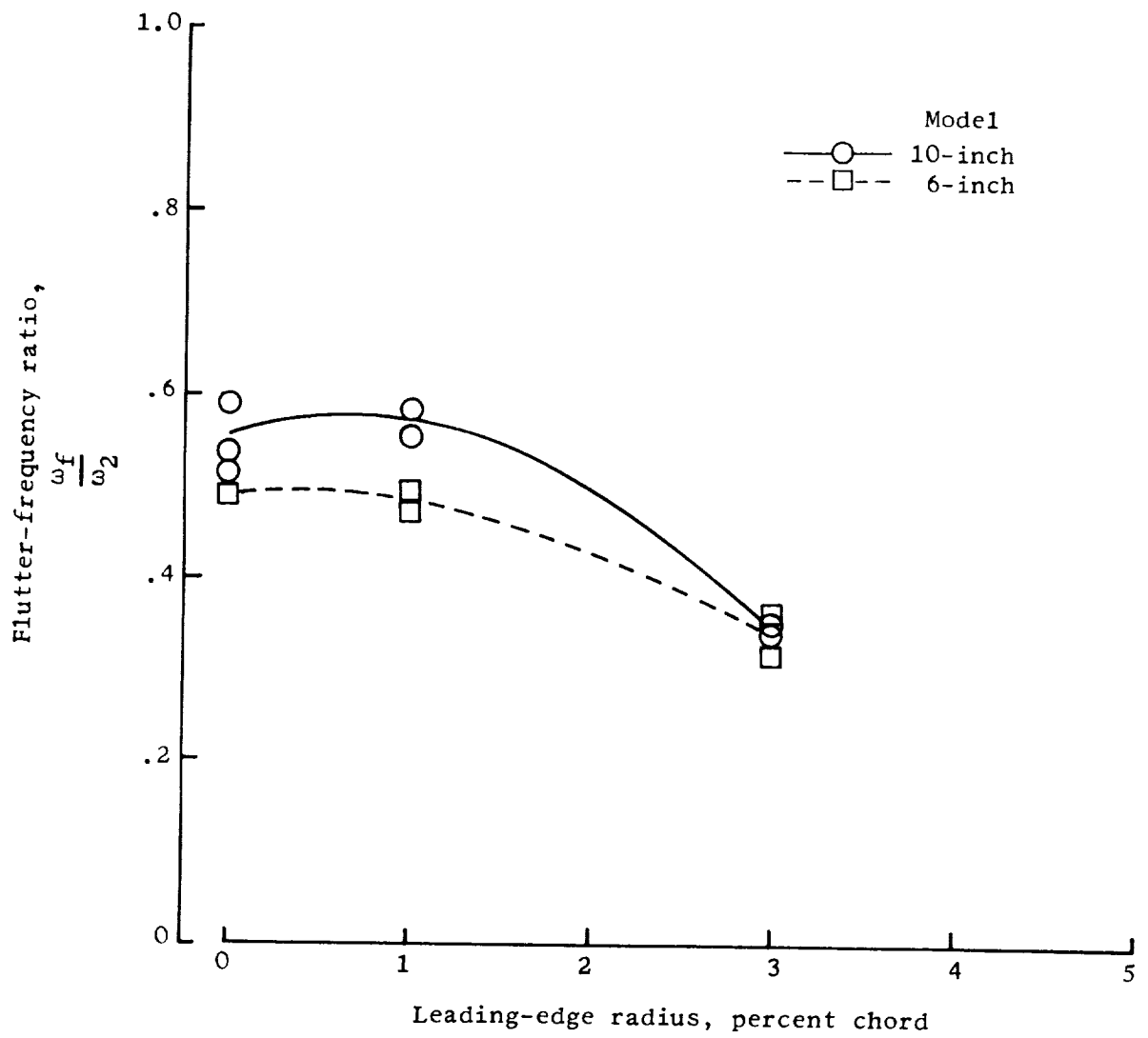


Figure 11.- Variation of flutter-frequency ratio with leading-edge radius.



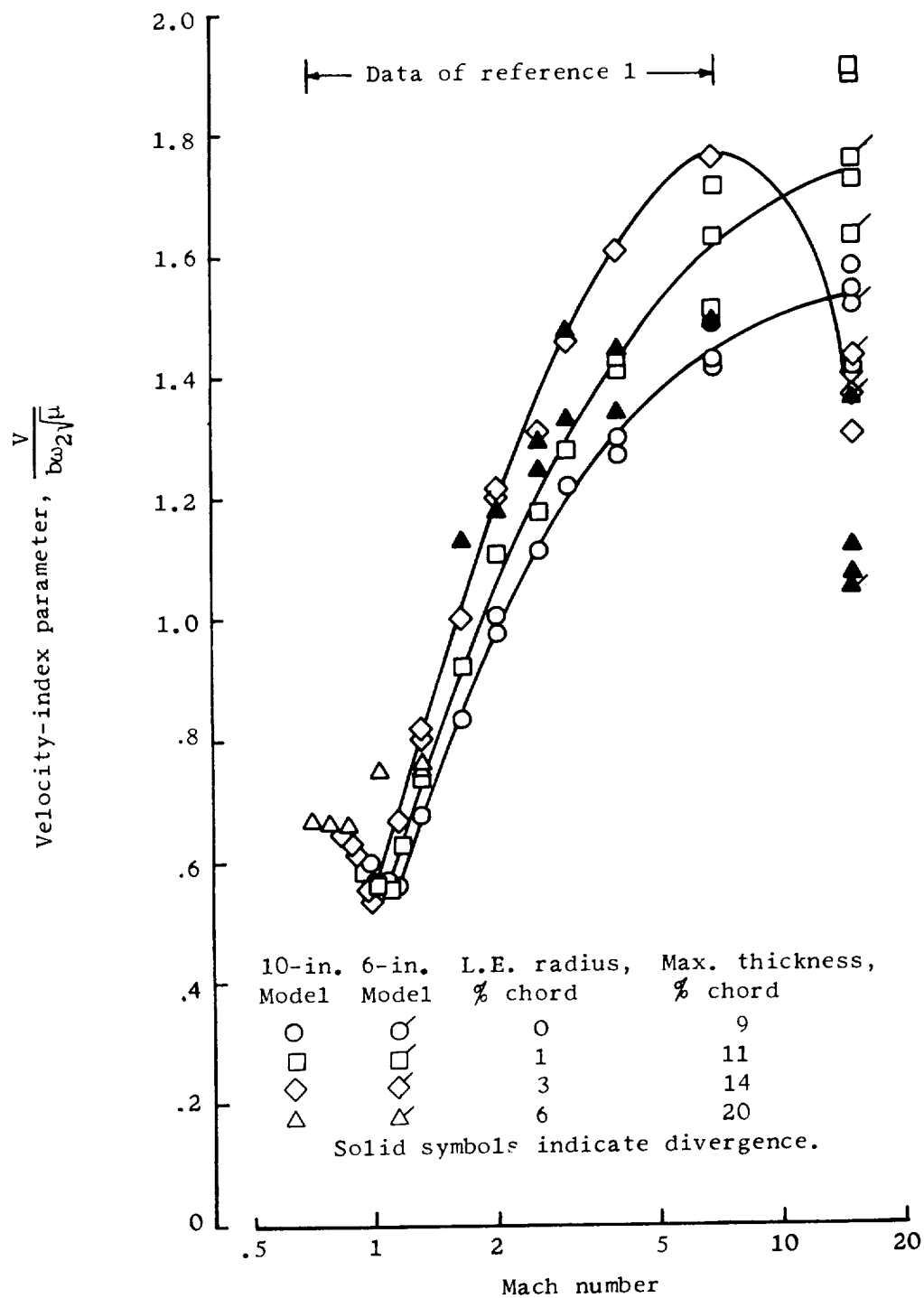


Figure 12.- Variation of velocity-index parameter with Mach number for double-wedge airfoils with blunt leading edges.

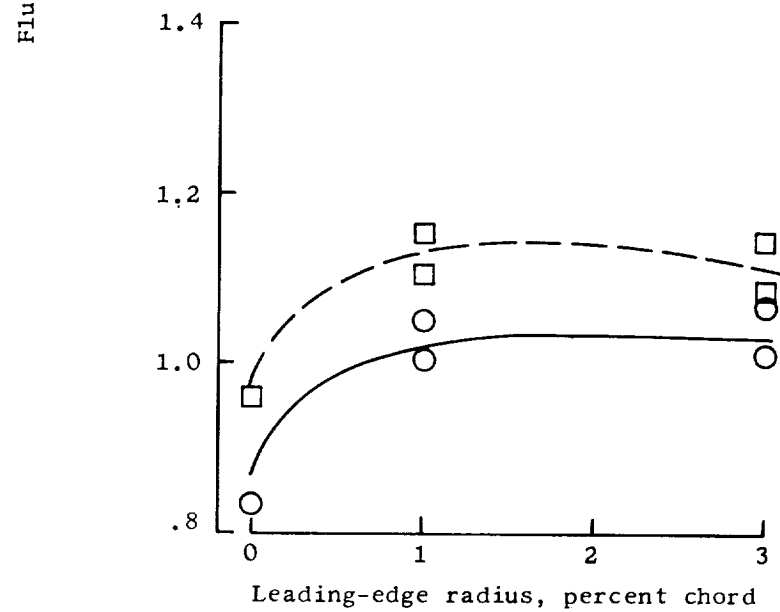
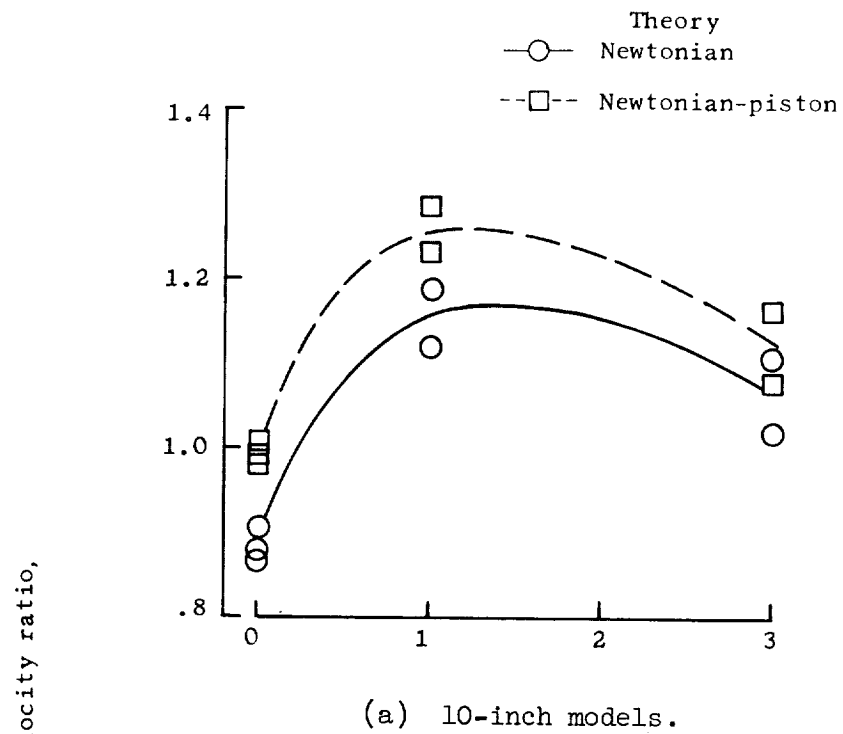


Figure 13.- Ratio of experimental to calculated flutter velocity as a function of leading-edge radius.

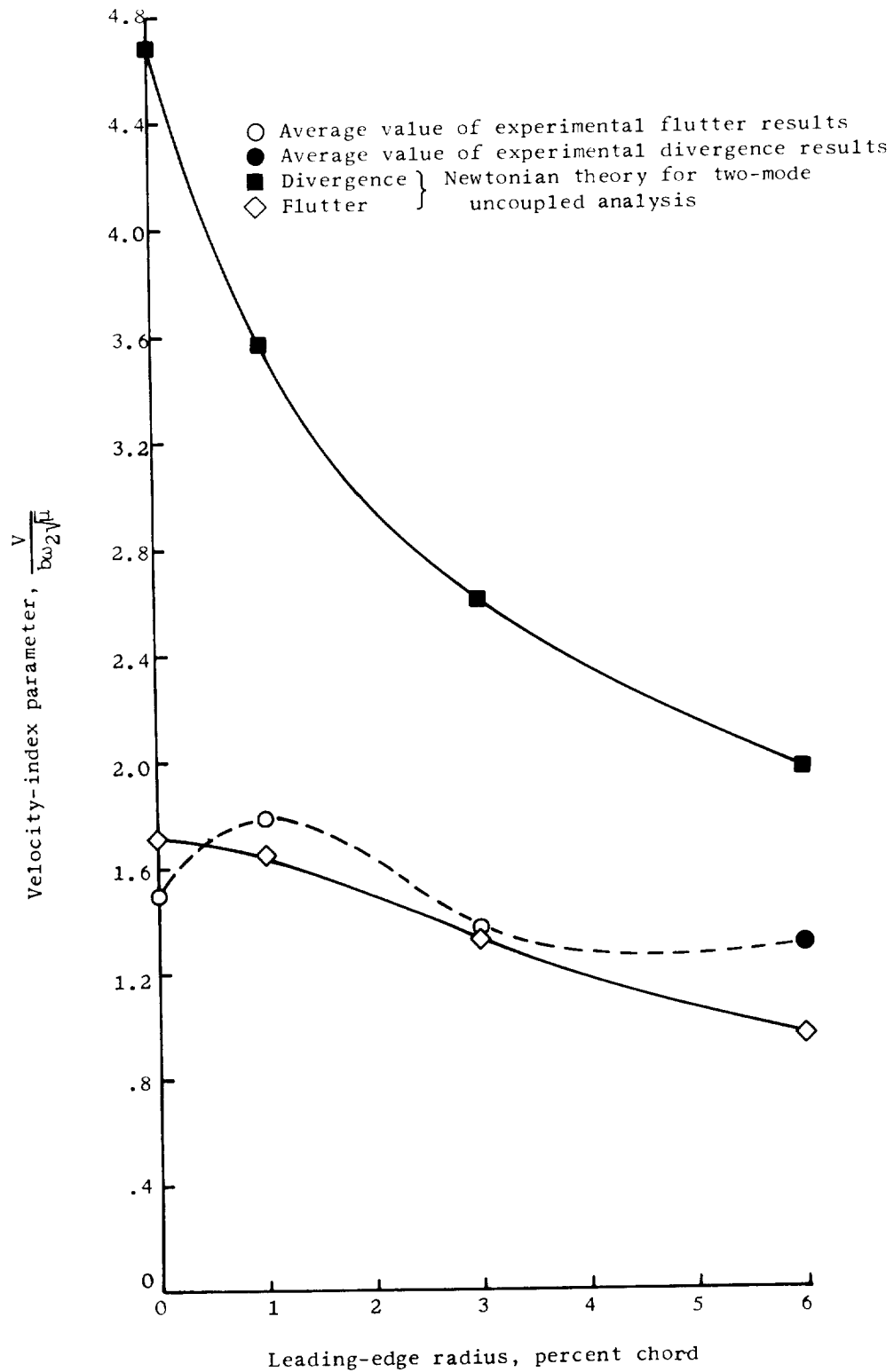
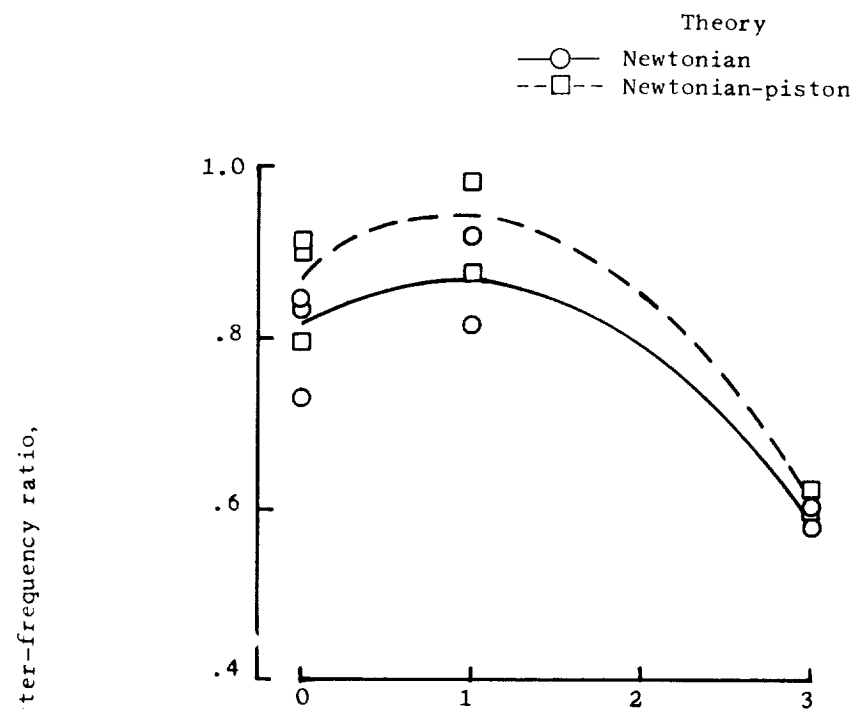
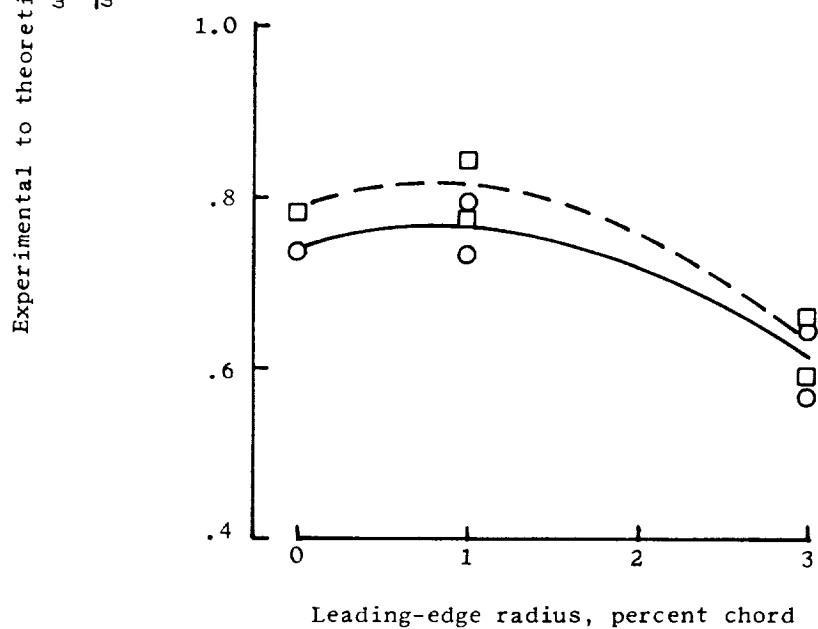


Figure 15.- Velocity-index trends with leading-edge bluntness.



(a) 10-inch models.



(b) 6-inch models.

Figure 14.- Variation of experimental to theoretical flutter-frequency ratio as a function of leading-edge radii.



